

# Modelling Ramp Losses and Magnetization in a Roebel-cable Based HTS Accelerator Magnet Prototype

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# Outline

- ▶ Motivation
- ▶ Methodology
- ▶ Results
- ▶ Conclusions

# Motivation

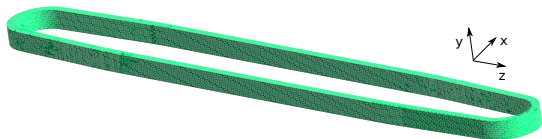


Figure: 3D depiction of FM-0

- ▶ 1st HTS Roebel-cable based R&D magnet: Feather M-0
- ▶ EuCARD-2 project lead by CERN
- ▶ Predicting magnetization and ramp losses is important
- ▶ Need for efficient modelling tools and methods arises

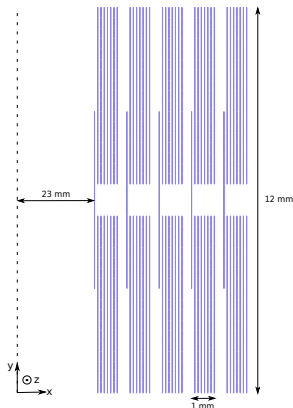


Figure: Modelling domain

## Methodology

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$$F(\Delta J) = \frac{1}{2} \Delta J^T M \Delta J$$

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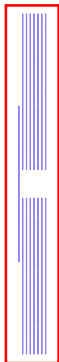
- ▶  $J$  limited by  $B$  (Kim model), or constant  $J_c$  (Bean model)
- ▶ Minimization carried out using Interior point optimizer (IPOPT)
- ▶ Simulation tool was programmed in C++ using the Riemannian manifold interface of Gmsh.



# Simulation approaches

► Bean model:

1. Ramp current constraint on each cable (Bean CC/cable)
2. Ramp current constraint on each tape (Bean CC/tape)



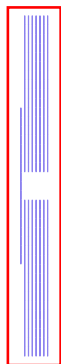
CC/cable



CC/tape

# Simulation approaches

- ▶ Bean model:
  1. Ramp current constraint on each cable (Bean CC/cable)
  2. Ramp current constraint on each tape (Bean CC/tape)
- ▶ Kim model:
  3. Ramp current constraint on each cable (Kim CC/cable)
  4. Ramp current constraint on each tape (Kim CC/tape)



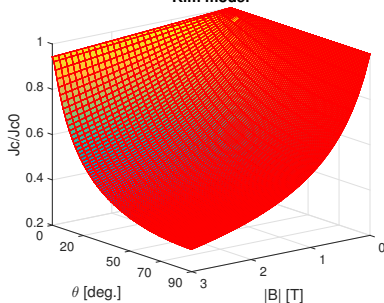
CC/cable



CC/tape

$$J_c(B_{\parallel}, B_{\perp}) = J_{c0} \left( 1 + \frac{\sqrt{k^2 B_{\parallel}^2 + B_{\perp}^2}}{B_0} \right)^{-\beta}$$

Kim model



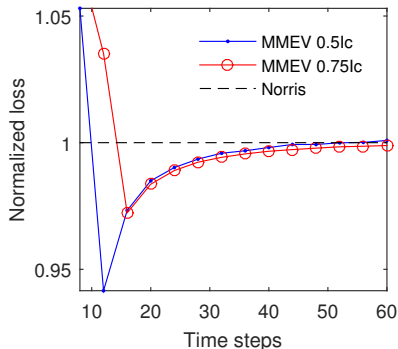
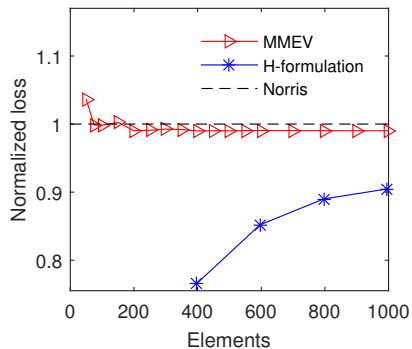
# Results

- ▶ Benchmarking against Norris strip formula
- ▶ Current distribution in modelling domain
- ▶ Magnetization in magnet's center
- ▶ Ramp losses

# Benchmarking against Norris strip formula: Bean model

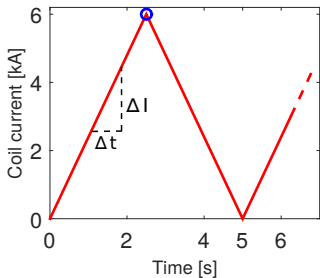
## ► Convergence analysis:

- Loss vs. elements
- Loss vs. time-steps (integrating  $P(t)$  over cycle)

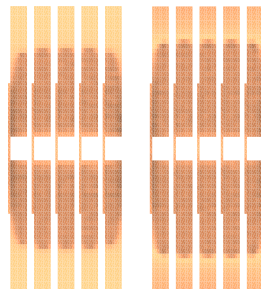


# Current distribution in modelling domain

- ▶ Current distributions were computed for each time-step
- ▶ Each  $\Delta t$  corresponds to change  $\Delta I$  in ramp current



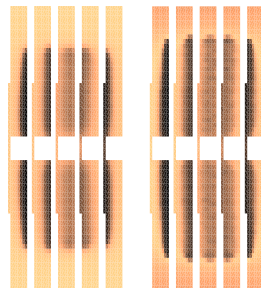
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Bean model

Kim model

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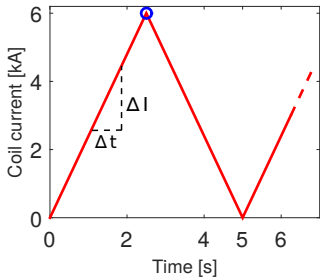


$-J_{co}$

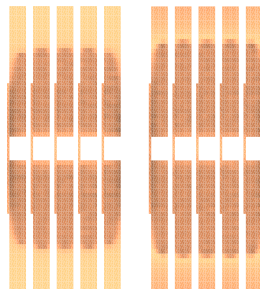
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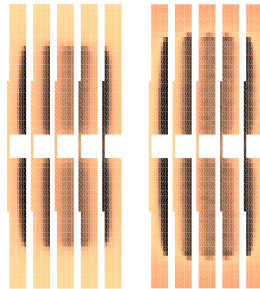
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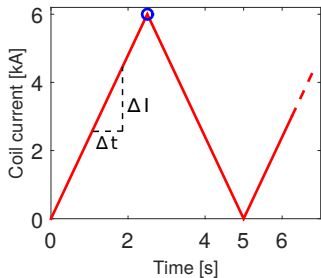


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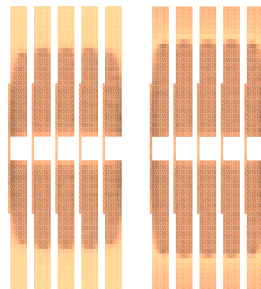
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- ▶ Coil  $I_c$  was determined with Kim model: 11.5 kA
- ▶ Cases result in different current penetration



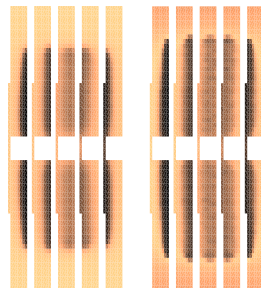
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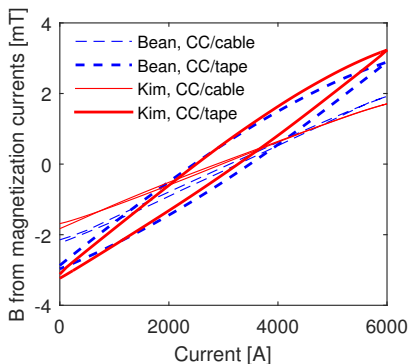
J<sub>co</sub>

## Magnetization in magnet's center

- ▶ Computed from the magnetization currents:  $J - J_{UNIFORM}$
- ▶ Tape-wise current condition resulted in largest magnetization field:  $\sim 3.2$  mT (Kim model)

Table: Kim CC/tape - normalized magnetization

CC/	Kim	Bean
tape	1	0.89
cable	0.53	0.59



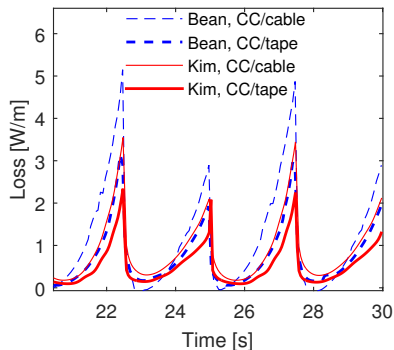
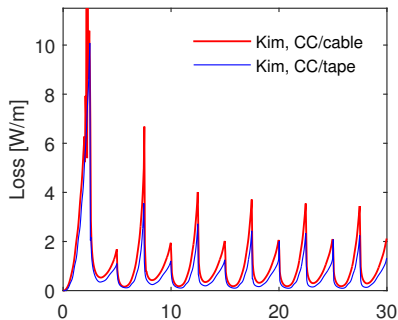


## Ramp losses

- ▶ Tape-wise current condition resulted in smallest loss per cycle:  $\sim 2.47$  J/m (Kim)

Table: Kim CC/tape - normalized ramp losses over cycle

CC/	Kim	Bean
tape	1	1.43
cable	1.75	2.18

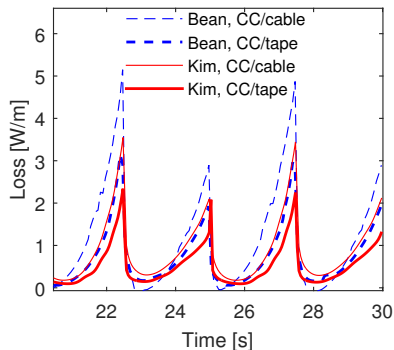
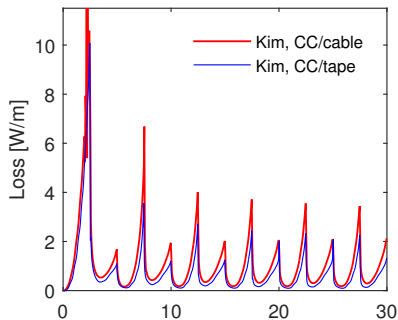


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- ▶ Tape-wise current condition resulted in smallest loss per cycle:  $\sim 2.47$  J/m (Kim)
- ▶ 27 km long string of magnets would generate  $\sim 67$  kWh heat energy per cycle (Kim CC/tape)

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- ▶ Real situation is in between these two current condition cases
  - ▶ Contact resistance
  - ▶ Transposition length
  - ▶ Current terminal

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- ▶ Experiments will give us more information
- ▶ MMEV-solver with IPOPT performed well
  - ▶ Outlook: Using parallelization, more complex magnets could be simulated rapidly



CHEERS!